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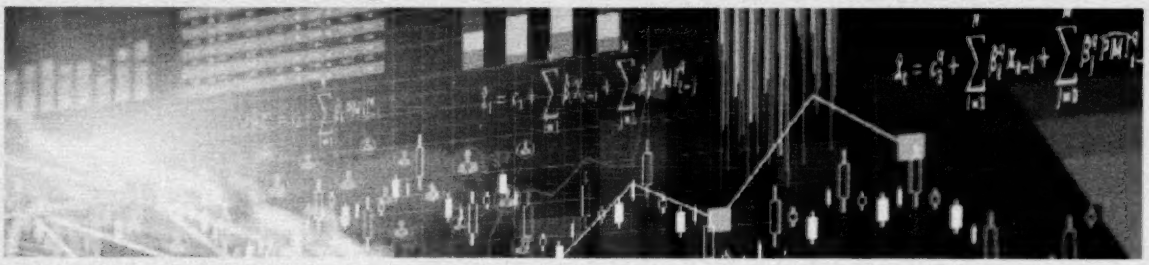
Agency Costs, Risk Shocks and International Cycles



by Marc-André Letendre and Joel Wagner

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Agency Costs, Risk Shocks and International Cycles

by

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Abstract

We add agency costs as in Carlstrom and Fuerst (1997) into a two-country, two-good international business-cycle model. In our model, changes in the relative price of investment arise endogenously. Despite the fact that technology shocks are uncorrelated across countries, the relative price of investment is positively correlated across countries in our model, much as it is in detrended U.S./euro area data. We also find that the financial frictions tend to increase the volatility of the terms of trade and the international correlations of consumption, hours worked, output and investment. We then compare this model to an alternative model that also includes risk shocks à la Christiano, Motto and Rostango (2014). We use credit spread data (for the United States) to calibrate the AR(1) process for risk shocks. We find that risk shocks are too small to significantly impact the model's dynamics.

JEL classification: E22, E32, E44, F44
Bank classification: Business fluctuations and cycles; International topics

Résumé

Dans un modèle de cycle économique à deux pays et à deux biens, nous intégrons des coûts de délégation à la manière de Carlstrom et Fuerst (1997). Dans notre modèle, les variations du prix relatif de l'investissement sont endogènes. Malgré l'absence de corrélation entre les chocs technologiques spécifiques aux pays, les prix relatifs de l'investissement sont positivement corrélés dans les deux pays, à l'instar de ce que l'on observe pour le couple États-Unis-zone euro dans les données dépouillées de leur composante tendancielle. Nous constatons également que les frictions financières ont tendance à accroître la volatilité des termes de l'échange et les corrélations de la consommation, des heures travaillées, de la production et de l'investissement entre pays. Nous comparons ensuite les résultats obtenus à ceux d'une variante du modèle dans laquelle sont incorporés des chocs de risque à la manière de Christiano, Motto et Rostango (2014). Nous employons des données relatives aux écarts de crédit aux États-Unis pour calibrer un processus autorégressif d'ordre 1 pour les chocs de risque. Il ressort de notre analyse que l'ampleur des chocs de risque est trop faible pour exercer une influence notable sur la dynamique du modèle.

Classification JEL : E22, E32, E44, F44
Classification de la Banque : Cycles et fluctuations économiques; Questions internationales

Non-Technical Summary

Motivation and Question

Standard international business cycle models fail to reproduce some of the stylized facts that characterize open economies. In particular, they cannot explain the positive cross-country correlation of main macroeconomic variables, including the price of investment relative to consumption goods (RPI), nor the high volatility of net exports and the terms of trade. This paper explores whether considering financial frictions can address these shortcomings.

Methodology

We introduce financial frictions into an otherwise standard two-country two-good international real business cycle model. Countries trade in the materials required to produce a final non-traded good, which can be either consumed as is, or be used as an input for investment production. Entrepreneurs, skilled in the task of producing investment goods, lack the funds required to meet investment demand and must partially rely on external financing. Since lenders have limited information about the creditworthiness of entrepreneurs, a risk premium is charged on the borrowed funds. This premium varies inversely with the entrepreneur's net worth. To assess the importance of financial frictions, we compute the main business cycle statistics implied by our model and compare them to both the standard model, as well as to the US/Euro Area data.

Key Contributions

We show that a model with financial frictions can account for the volatility of net exports and the terms of trade as well as for the cross-country correlation in economic aggregates and the RPI. During domestic economic expansions, investment demand increases faster than entrepreneurs' net worth, causing lenders to charge a higher premium on borrowed funds. The higher premium in turn translates into higher RPI, causing households to forgo some of their investment purchases. As domestic demand for their own locally produced intermediate goods decreases, their supply on international markets rises and the price of exports declines. For the foreign country, the drop in import prices stimulates economic activity and boosts the foreign RPI, while the terms of trade depreciate above and beyond that predicted by a model that ignores financial frictions. Hence, through all these mechanisms, financial frictions bring the predicted cross-country correlations closer to the ones observed in data, improving the performance of the standard model.

Future research

In the literature, movements in the RPI have been traditionally assumed to reflect shifts in technology. However, as demonstrated in this paper, when financial frictions are considered, the RPI also responds to shifts in investment demand. This suggests that the current literature might overestimate the importance of technological progress in driving investment. We plan to use our more general framework to reassess the contribution of investment-specific technology shocks to business cycle volatility.

1 Introduction

The seminal work on international real business cycles by Backus, Kehoe and Kydland (BKK 1992) highlighted three puzzling facts that separate their model from the data. The first of these puzzles has been referred to as the "quantity anomaly" (in BKK, the cross-country correlation of output is less than the cross-country correlation of consumption, a phenomenon not observed in the data). The second anomaly concerns cross-country correlations of investment and hours worked (they are positive in the data but negative in BKK). The third anomaly pointed out by BKK highlights their model's inability to adequately capture volatility in the terms of trade and net exports simultaneously. This phenomenon has been coined as the "price anomaly."

In the literature, there have been several attempts to address the puzzles/anomalies listed above.[1] Recent attempts to bring the BKK model closer to the data have done so by incorporating investment-specific technology into the list of exogenous shocks included in the model. Since its conception by Greenwood, Hercowitz and Huffman (GHH, 1988), the standard method has been to identify investment-specific technology by the inverse of the relative price of investment (RPI). The motivation for this method is simple. If there exists a perfectly competitive firm converting consumption goods into investment goods via an investment-specific technology (IST), then the RPI can be used to perfectly identify movements in IST. Thus, by assuming that IST is an exogenous shock, we also assume that the RPI is orthogonal to any and all other forms of economic disturbances. This assumption, however, seems unlikely since, as Schmitt-Grohé and Uribe (2011) point out, both neutral and investment-specific technology follow a common stochastic trend in the postwar United States. Likewise, Floetotto et al. (2009) point out that by assuming that IST is an exogenous technology shock, we are assuming that the RPI does not respond to variations in investment demand over the course of the business cycle. Fisher (2009) highlights this problem by emphasizing that if there exists any asymmetries separating the investment- and consumption-producing sectors, this can be problematic when identifying IST by the inverse of the RPI. Thus, suggesting the typical method for identifying IST that has been in place since GHH (1988) may be inappropriate.

The ability of IST shocks to generate realistic business cycles is questionable. Justiniano, Primiceri and Tambalotti (2011) demonstrate that in a closed-economy framework, when IST technology is properly calibrated to match the observed fluctuations in the RPI, IST shocks lose their ability to generate business-cycle volatility. A similar debate has been going on in the international business-cycle literature. Raffo (2010) adds IST shocks to a BKK-style model. He finds that adding IST shocks to the model solves the puzzles listed in our opening paragraph. A significant drawback in his analysis is that the IST shocks in his model are not tied to RPI data. Mandelman, Rabanal, Rubio-Ramírez and Vilán (2011) also look at the role of IST shocks in a BKK-style model. They use RPI data for the United States and

[1] See, for example, Baxter and Crucini (1995), Stockman and Tesar (1995), Boileau (2002), Heathcote and Perri (2002), Benigno and Thoenissen (2008), Corsetti, Dedola and Leduc (2008), Raffo (2010) and Mandelman, Rabanal, Rubio-Ramírez and Vilán (2011) to name a few.

the "rest of the world" to estimate the stochastic process for IST shocks included in their model. They find that IST shocks are not powerful enough to resolve these puzzles. One of our contributions is to revisit this debate. Much as Mandelman et al. (2011), we find that IST shocks do little to improve canonical international business-cycle predictions.

Our first central contribution to the literature is related to the debate above. By including agency costs as in Carlstrom and Fuerst (CF) (1997) in a two-country, two-good model,[2] the RPI is entirely endogenous and fluctuates in response to technology shocks (the only disturbances included in the model). We show that these financial frictions increase the variance of the terms of trade and cross-country correlations.[3] Our model is able to produce positive cross-country correlations *despite the fact that technology shocks are completely uncorrelated across countries.* Furthermore, these encouraging results are obtained in a context where the volatility of the RPI and its cross-country correlations resemble their counterparts in the data. The relative standard deviation of the RPI is about 25% smaller than in U.S. data. Trade in intermediate goods causes a transmission of agency costs across countries, which produces a small positive correlation of the RPI across countries – much like in our U.S./euro-area data. Our work suggests that our model with agency costs does better than a model with IST shocks,[4] with the additional advantage that the RPI is actually explained by the model. Below, we provide more details about the model and its inner workings.

Our second central contribution relates to risk shocks. This concept was developed by Christiano, Motto and Rostango (2014), who include risk shocks into an otherwise standard Bernanke, Gertler and Gilchrist (1999) costly state-verification framework. As in their paper, a positive risk shock in our model increases the cross-sectional dispersion of the entrepreneur's idiosyncratic productivity, which in turn increases the uncertainty regarding the probability of entrepreneurial failure. Christiano, Motto and Rostango (2014) find that disturbances to this degree of uncertainty, referred to as "risk shocks," lead to realistic business-cycle dynamics in a closed-economy environment. Our analysis shows that risk shocks have the potential to raise the volatility of the RPI and that of the terms of trade (TOT). However, in our model, risk shocks lead to responses of output, consumption, investment and hours worked that are of opposite signs across countries. This is not a desirable feature, given the model's natural inability to produce positive cross-country correlations. We use credit spreads between rates on U.S. Baa corporate bonds and 10-year U.S. government bonds to calibrate the bivariate AR(1) process driving the variance of entrepreneurial productivity. The variance of the spreads in our model matches the variance of the spreads in the data. We find that risk shocks are actually not large enough to materially change the statistical moments implied by our benchmark model.

Why use financial frictions to generate endogenous movements in the RPI, both within

[2] We elected to use the CF (1997) model over other costly state-verification models since it allows for endogenous movements in the RPI.

[3] Yao (2012) documents the effects of a leverage constraint on international correlations in an extended one-good BKK model.

[4] Where IST shocks are tied to RPI data.

and across countries? In the simplest stochastic dynamic general-equilibrium models, a representative agent can convert one unit of consumption good into one unit of capital ready for production. This very simple capital accumulation process can be made more realistic by breaking it into two stages. In the first step, a technology is employed to convert consumption goods into investment goods. Shocks hitting that technology are known as the IST shocks mentioned above. For example, shocks that lower costs in the investment sector, such as advancements in computer processing or improvements in production methods, are of the IST type. In the second stage, investment goods are transformed into productive capital before entering the production process. Shocks that hit this transformation process are known as shocks to the marginal efficiency of investment (or MEI shocks). For example, shocks that affect the dissemination of investment goods, such as new forms of transportation or troubles in the financial sector, are of the MEI type.

One of the most obvious impediments to acquiring capital is the credit needed to purchase investment goods. Disturbances to the credit market, including the recent financial crisis, affect the ability of firms to acquire capital, with consequences for the course of the economy. In their empirical work using U.S. data, Justiniano, Primiceri and Tambalotti. (2011) identify MEI shocks as the primary source of business-cycle volatility, accounting for 60% of the variation in U.S. GDP, while IST shocks account for only a small fraction of that variance. Moreover, Schmitt-Grohé and Uribe (2012) estimate a closed-economy model that includes an extensive list of anticipated and unanticipated shocks. They conclude that MEI shocks are "estimated to explain a significant fraction of the variation in output (28%) and investment (63%)" in the United States.[5] Given those empirical results, it is of interest to see how financial frictions change the dynamics of an international business-cycle model. It is worth noting that there is evidence that total factor productivity (TFP) and the RPI are interrelated in the United States (e.g., Schmitt-Grohé and Uribe, 2011). These two variables are intimately related in our theory, since TFP shocks eventually lead to changes in the RPI.

As highlighted above, our model is capable of reproducing international co-movements in the RPI despite the fact that innovations in TFP are not correlated across countries. To understand why the RPI is positively correlated across countries, consider an unexpected positive productivity shock in country 1 in period 1. Since this shock is persistent, households desire to increase their capital stock–hence, they demand more investment goods. In light of this, entrepreneurs increase the size of their projects. Given that their net worth is mostly predetermined, they must borrow more. This greater reliance on external funds raises agency costs, and the price of investment goods in terms of the final good shoots up. This tempers country 1's demand for investment goods, leading to more units of that country's intermediate good finding their way to the world market. This results in a more important depreciation of the terms of trade than in the BKK model. The significant drop in the price of country 1's good prompts country 2 to buy more of it to raise consumption and investment (consumption smoothing). This increase in the demand for investment goods in country 2 pushes agency costs up, which raises the RPI in that country. These initial positive responses of the price of investment in both countries promote positive correlations

[5]Schmitt-Grohé and Uribe (2012), p. 2759.

in our simulations.

The remainder of the paper is organized as follows. Section 2 lays out our model with agency costs. We explain how we select parameter values in Section 3. Section 4 discusses the benchmark model's implications. Section 5 covers a model with IST shocks and one with risk shocks. Sensitivity analysis is done in Section 6. Section 7 concludes.

2 Benchmark Model

Our model is based on the two-country, two-good international real business-cycle model of BKK (1994). It consists of two countries that trade intermediate goods and financial assets. Each country has a large number of identical households, a large number of perfectly competitive and identical intermediate goods producers and a large number of perfectly competitive and identical final goods producers. Each country produces a single intermediate good. Intermediate goods from both countries are needed to produce final goods. Final goods are not traded internationally and can be either consumed or used as inputs in the production of new physical capital.

We extend the BKK (1994) model by adding to each country (i) a financial sector that contains a large number of perfectly competitive and identical capital mutual funds (CMFs) and (ii) a set of entrepreneurs that produce the physical capital in the economy. As in CF (1997), the idiosyncratic productivity of entrepreneurs is private information, which gives rise to agency costs. These agency costs lead to endogenous changes in the RPI. The next few subsections provide a detailed description of the model.

2.1 Intermediate goods sector

Let l index countries, where $l \in \{1, 2\}$. Within each country, there are a large number of identical and perfectly competitive intermediate goods producers. Hence, we restrict our attention to a representative producer. Each country specializes in the production of an intermediate good. Country 1 (or the home country) produces intermediate good a (one can think of this as aluminum) and country 2 (or the foreign country) produces good b (one can think of this as bricks). These goods are traded across countries. We let q_{lt} (q^*_{lt}) denote the price of the intermediate good produced in country l in terms of the final good in country 1 (country 2).

The production of intermediate goods requires capital and labour, which are assumed to be immobile across countries. The representative producer in country l rents the economy's

entire capital stock[6] available at the beginning of period t (K_{lt}) and hires the labour services supplied by households (H_{lt}) to produce intermediate goods according to the production function

$$Y_{lt} = Z_{lt} K_{lt}^{\alpha_K} (H_{lt})^{\alpha_H}, \qquad l = \{1, 2\}, \tag{1}$$

where $0 < \alpha_k, \alpha_H < 1$, $\alpha_k + \alpha_H = 1$ and Z_{lt} denotes an unanticipated stationary productivity shock. The representative intermediate good producer in country 1 maximizes

$$\Pi_{1t} = q_{1t} Y_{1t} - w_{1t} H_{1t} - r_{1t} K_{1t} \tag{2}$$

subject to (1) for $l = 1$. The producer rents capital from both households and entrepreneurs at a rental rate r_1 and hires household labour at the wage rates w_1. Owing to the constant returns-to-scale production function and perfectly competitive markets, the wage and rental rates of labour and capital are equal to their corresponding marginal product.

2.2 Households

Each country is populated by a large number of identical, infinitely lived households. We assume that the household population in each country is normalized to 1. The representative household in country $l = \{1, 2\}$ has the following expected lifetime utility function

$$E_0 \sum_{t=0}^{\infty} \beta^t \frac{[C_{lt}^H - \psi H_{lt}^{\nu} X_{lt}]^{1-\gamma}}{1-\gamma}, \qquad 0 < \beta < 1,\ \nu > 1,\ \psi > 0, \tag{3}$$

where

$$X_{lt} = C_{lt}^{H\eta} X_{lt-1}^{1-\eta}, \qquad 0 \leq \eta \leq 1. \tag{4}$$

We denote consumption by C_{lt}^H and labour supply by H_{lt}. Whether or not consumption and hours worked by the household are time separable is determined by η, through the inclusion of X_{lt} in the household's utility function. These preferences were first proposed by Jaimovich and Rebelo (2009). This allows us to dial up or down the strength of the wealth effect on the household's labour supply decision. When $\eta = 1$ (full wealth effect), these preferences become equivalent to the widely used preferences of King, Plosser and Rebelo (KPR) (1988). When $\eta = 0$ (no wealth effect), they become equivalent to those in GHH (1988).

The representative household in country 1 must satisfy the budget constraint

$$C_{1t}^H + P_{1t} I_{1t}^H + q_{1t} \Sigma_{s^{t+1}} M(s^t, s_{t+1}) D_1(s^t, s_{t+1}) = w_{1t} H_{1t} + r_{1t} K_{1t}^H + q_{1t} D_1(s^{t-1}, s_t) + PR_t. \tag{5}$$

The left side of the equation reflects the fact that the household uses its income for three purposes: to consume, invest, and insure. Households can increase their capital stock by purchasing I_{1t}^H units of new investment goods at a unit cost P_{1t}. Here, P_{1t} represents the

[6] Uppercase variables denote aggregate variables, whereas lowercase variables are specific to an individual agent.

price of new investment goods in country 1 relative to the price of that country's final good. The price of new investment goods is taken as given by households (just like all other prices). Lastly, households trade state-contingent (Arrow-Debreu) securities. We can imagine that households are the ones deciding how many units of intermediate goods to import or export. Accordingly, they will trade contingent claims with households in the other country to cover any trade balance deficit. Let $D_1(s^t, s_{t+1})$ be the quantity of contingent claims purchased by households in country 1 after history s^t, which pays one unit of good a in period $t+1$ when the state of the economy is s_{t+1}. We denote the price of these contingent claims (in units of good a) by $M(s^t, s_{t+1})$.

The right side of equation (5) shows that the representative household income in period t consists of its labour income $w_{1t}H_{1t}$, rental income $r_{1t}K_{1t}^H$, payoffs $D_1(s^{t-1}, s_t)$ from the relevant state-contingent security purchased in the previous period and the collective profits of all domestic firms. The budget constraint of the representative household in country 2 is analogous.

The representative household capital accumulation equation is

$$K_{1t+1}^H = (1-\delta)K_{1t}^H + I_{1t}^H, \tag{6}$$

where δ is the depreciation rate. The representative household chooses the sequences of consumption, labour, contingent claims and investment that maximize their lifetime utility (3) subject to equations (4) through (6), taking all prices as given.

2.3 Final goods sector

Each country has a large number (measure one in each country) of identical and perfectly competitive final goods[7] producers. Hence, we restrict our attention to a representative final goods producer. Each country specializes in the production of a non-traded final good, which is used for household and entrepreneurial consumption and as an input in the production of investment goods. Production of the final good requires both domestic and imported intermediate goods. Country 1's production of its final good is given by the following Armington (1969) aggregator

$$G(a_{1t}, b_{1t}) = \left[\kappa a_{1t}^{\frac{\sigma-1}{\sigma}} + (1-\kappa) b_{1t}^{\frac{\sigma-1}{\sigma}}\right]^{\frac{\sigma}{\sigma-1}}, \qquad 0 < \kappa < 1, \quad \sigma > 0. \tag{7}$$

When $\kappa > 0.5$, each country has a bias towards the domestically produced intermediate good. Here σ represents the elasticity of substitution between domestic and foreign goods.

The representative final good producer in country 1 chooses quantities a_1 and b_1 to maximize its profits given by $G(a_{1t}, b_{1t}) - q_{1t}a_{1t} - q_{2t}b_{1t}$. Similarly, the foreign final good

[7] We use "final goods" and "consumption goods" interchangeably.

producer chooses a_2 and b_2 to maximize $G(b_{2t}, a_{2t}) - q_{1t}^* a_{2t} - q_{2t}^* b_{2t}$ where

$$G(b_{2t}, a_{2t}) = [\kappa b_{2t}^{\frac{\varrho-1}{\varrho}} + (1-\kappa) a_{2t}^{\frac{\varrho-1}{\varrho}}]^{\frac{\varrho}{\varrho-1}}. \tag{8}$$

2.4 The entrepreneurs

Each country is populated by an infinite number of entrepreneurs (measure one in each country). Entrepreneurs are not identical. The efficiency of the process employed by an entrepreneur to transform consumption goods (the final good in this model) into investment goods is specific to each entrepreneur and is determined by the random variable ω. The latter is assumed to be independently and identically distributed across entrepreneurs with a lognormal cumulative distribution function $\Phi(\omega)$ and density function $\phi(\omega)$. An entrepreneur with productivity ω transforms (within one period) i units of the consumption good into ωi units of investment goods. The resources required by entrepreneurs to fund the investment projects come from their own net worth n (internal funds), as well as from funds borrowed (via intra-period loans) from financial intermediaries (CMFs). Intermediaries obtain funds from households.

To introduce agency costs into our model, we assume that each entrepreneur's random productive potential, ω, is private information. If a CMF wishes to observe an entrepreneur's level of productivity, it must incur a monitoring cost μi, which is measured in units of investment goods. Owing to this asymmetric information, there is a moral hazard problem between borrowers/entrepreneurs and their potential lenders. The model is set up such that entrepreneurs will always truthfully report their ω.

An individual entrepreneur living in country l maximizes their expected lifetime utility given by,

$$E_0 \sum_{t=0}^{\infty} (\beta\Gamma)^t c_{lt}^E \qquad 0 < \Gamma < 1, \tag{9}$$

where c_{lt}^E is the entrepreneur's level of consumption. The assumption $0 < \Gamma < 1$ implies that entrepreneurs are relatively more impatient than households. This assumption, which is common in this literature, is made to avoid scenarios where entrepreneurs fully finance their investment projects by dramatically reducing their level of consumption.

Entrepreneurs face a budget constraint. An important component of that constraint is net worth. At the beginning of period t, an entrepreneur rents out their current capital stock (denoted k_{lt}^E) to local intermediate goods producers, which generates rental income $r_{lt} k_{lt}^E$. Then, the entrepreneur sells off all of their undepreciated capital stock $(1-\delta)k_{lt}^E$ to the local CMF, which pays $P_{lt}(1-\delta)k_{lt}^E$ units of consumption goods to the entrepreneur. After all these transactions, an entrepreneur in country $l = \{1, 2\}$ has a total net worth (measured in

units of domestic consumption goods) of:

$$n_{lt} = r_{lt} k_{lt}^E + P_{lt}(1-\delta) k_{lt}^E. \tag{10}$$

In the next section, we outline the financial contract between entrepreneurs and the CMF. But for now, it is enough to state that the net worth of an entrepreneur is inversely related to the interest rate charged on loans. Hence, a rational risk-neutral entrepreneur always chooses to sell off all of its undepreciated capital supply to bolster net worth. The income earned from the production of investment goods, discussed in the next subsection, constitutes the last element required to determine an entrepreneur's budget.

2.4.1 Financial contract and investment decision

Since country l's entrepreneurs are dealing with country l's CMFs exclusively (and *vice versa*), we momentarily omit the country subscript on variables to ease notation. Similarly, since loan contracts are entirely "resolved" within a period, we also omit time subscripts. Entrepreneurs are indexed by j. For example, entrepreneur j's productivity is denoted by ω_j.

Asymmetric information in our model becomes relevant only when an entrepreneur's net worth is low enough that they must partially rely on external financing from the CMF. In that context, an entrepreneur with net worth n_j that invests i_j must borrow $(i_j - n_j)$ units of consumption goods from the CMF in order to start production. The sequence of events within a period is borrowed from CF:

(i) Entrepreneur j and a CMF enter into a contractual agreement whereby investment i_j is determined. Given entrepreneurial net worth n_j, the amount borrowed $(i_j - n_j)$ is also determined.

(ii) Productivity ω_j is realized. Based on this realization, the entrepreneur decides whether to honour their contract. The latter decision rests on a threshold productivity level $\bar{\omega}_j$ defined below. More specifically, if $\omega_j \geq \bar{\omega}_j$, the entrepreneur repays the CMF. Otherwise, the entrepreneur defaults on the loan, which triggers monitoring by the CMF and confiscation of all of the investment goods just produced by the entrepreneur.

(iii) Entrepreneurs that did not default make their consumption decision.

Despite the heterogeneity of the entrepreneurial population, asymmetric information implies that the CMF charges a common interest rate r^k on all funds borrowed by entrepreneurs. Thus, an entrepreneur that borrows $(i_j - n_j)$ units of consumption goods from the CMF in any given period (and does not default) has to pay back $(i_j - n_j)(1 + r^k)$ units of investment goods to the CMF in that same period.

As mentioned in point (ii) above, there exists a productivity threshold $\bar{\omega}_j$ at which entrepreneur j is indifferent between defaulting or repaying the loan to the CMF. This indifference point is reached when the quantity of investment goods produced by the entrepreneur is exactly equal to the amount owed to the CMF. Hence, $\bar{\omega}_j$ is the value of ω_j for which

$$i_j \bar{\omega}_j = (i_j - n_j)(1 + r^k) \quad \Rightarrow \quad \bar{\omega}_j = (1 + r^k)(1 - n_j/i_j). \tag{11}$$

Any productivity realization ω_j less than $\bar{\omega}_j$ leads entrepreneur j to default.

Given the definition of $\bar{\omega}$ provided above, we can now calculate entrepreneur j's expected net income (before idiosyncratic risk is resolved, *i.e.*, before ω_j is observed) associated with the production of investment goods

$$F_j^E = P \left(\int_{\bar{\omega}_j}^{\infty} \omega \, i_j \, \phi(\omega) \mathrm{d}\omega - (1 - \Phi(\bar{\omega}_j))(1 + r^k)(i_j - n_j) \right). \tag{12}$$

The first term in parentheses calculates the expected output of investment goods when entrepreneur j does not default. From this quantity, we subtract the expected amount that must be repaid to the CMF. Recall that when an entrepreneur defaults on their loan, their entire output is confiscated by the CMF, leaving them with a net income of zero.

Expected income can be written as follows using (11):

$$F_j^E = P \, i_j \underbrace{\left(\int_{\bar{\omega}_j}^{\infty} \omega \phi(\omega) \mathrm{d}\omega - [1 - \Phi(\bar{\omega}_j)] \bar{\omega}_j \right)}_{\equiv f(\bar{\omega}_j)} = P \, i_j f(\bar{\omega}_j). \tag{13}$$

Similarly, the expected income of the CMF in its dealings with entrepreneur j is given by

$$F_j^{CMF} = P \left(\int_0^{\bar{\omega}_j} \omega i_j \phi(\omega) \mathrm{d}\omega - \Phi(\bar{\omega}_j) \mu i_j + (1 - \Phi(\bar{\omega}_j))(1 + r^k)(i_j - n_j) \right), \tag{14}$$

where income is calculated in units of consumption goods. The first two terms in parentheses calculate the expected amount the CMF confiscates when the entrepreneur defaults, net of the expected monitoring costs. The last term accounts for the expected payment made when entrepreneur j does not default.

Expected income can be written as follows using (11):

$$F_j^{CMF} = P \, i_j \underbrace{\left(\int_0^{\bar{\omega}_j} \omega \phi(\omega) \mathrm{d}\omega - \Phi(\bar{\omega}_j) \mu + [1 - \Phi(\bar{\omega}_j)] \bar{\omega}_j \right)}_{\equiv g(\bar{\omega}_j)} = P \, i_j g(\bar{\omega}_j). \tag{15}$$

Quantities $f(\bar{\omega}_j)$ and $g(\bar{\omega}_j)$ refer to the fraction of expected net capital output going to the entrepreneur and the CMF, respectively. Assuming $E[\omega] = 1$ (a normalization), one can

easily show that

$$f(\bar{\omega}_j) + g(\bar{\omega}_j) = 1 - \Phi(\bar{\omega}_j)\mu. \tag{16}$$

So far, we have set up the general form of the contract, fully identified by the level of consumption goods used in investment production (i_j), and the threshold $\bar{\omega}_j$ with a gross interest rate charged on borrowed funds of

$$1 + r^k = \frac{\bar{\omega}_j}{1 - n_j/i_j}, \tag{17}$$

which is implied by (11).

Following CF, we assume that the lender is unaware of the entrepreneur's previous history, eliminating any repeated game scenario. Recall our assumption that ω is i.i.d. over time. Therefore, each contract is relevant for the current period only. From one of the many potential contracts, there exists an optimal contract that maximizes the expected income to the entrepreneur while leaving the lender indifferent between lending or retaining the necessary funds. Therefore, the optimal contract is the pair $(i_j, \bar{\omega}_j)$ maximizing F_j^E subject to

$$F_j^{CMF} \geq (i_j - n_j). \tag{18}$$

This optimization problem implies

$$i_j = \frac{n_j}{(1 - Pg(\bar{\omega}_j))} \tag{19}$$

and

$$P\left\{1 - \Phi(\bar{\omega}_j)\mu + \frac{\phi(\bar{\omega}_j)\mu f(\bar{\omega}_j)}{f'(\bar{\omega}_j)}\right\} = 1. \tag{20}$$

Since each entrepreneur takes the RPI as given, equation (20) implies that $\bar{\omega}_j$ is an implicit function of the relative price P. Since the relative price is the same for all entrepreneurs, we have $\bar{\omega}_j = \bar{\omega}$ for all j. Furthermore, given $\bar{\omega}(P)$, equation (19) determines the optimal amount of investment by the entrepreneur. This can be written as a function of the entrepreneur's wealth and the relative price of investment

$$i_j = \frac{n_j}{1 - Pg(\bar{\omega}(P))} \equiv i(P, n_j). \tag{21}$$

Before turning to the consumption decision of an entrepreneur, we derive the aggregate amount of investment goods produced and supplied within a country. Entrepreneur j's choice $i(P, n_j)$ indicates the quantity of *consumption goods* the entrepreneur decides to use as input in the production of investment goods. The expected quantity of *investment goods* produced and supplied by entrepreneur j, net of monitoring costs when $\omega_j < \bar{\omega}$, is given by

$$i^s(P, n_j) \equiv i(P, n_j)\{1 - \mu\Phi(\bar{\omega}(P))\} = \frac{1 - \mu\Phi(\bar{\omega}(P))}{1 - Pg(\bar{\omega}(P))} n_j. \tag{22}$$

Since the price of capital P is taken parametrically, an entrepreneur's choice of $i^s(P, n_j)$ is a linear function of their net worth n_j, which is convenient from the point of view of aggregation. Given our assumption of an infinite number of entrepreneurs (with measure unity), the law of large numbers implies that the above formula can be interpreted as the total amount of investment goods supplied by the population of entrepreneurs when total entrepreneurial net worth turns out to be n_j. Accordingly, denoting total entrepreneurial net worth by N, the supply of investment goods in the entire country is given by

$$I^S(P, N) = \frac{1 - \Phi(\bar{\omega}(P))\mu}{1 - Pg(\bar{\omega}(P))} N. \tag{23}$$

Bringing back country and time subscripts, the supply of investment goods in country l in period t is given by

$$I^S_{l,t} = \frac{1 - \Phi(\bar{\omega}_{lt})\mu}{1 - P_{lt} g(\bar{\omega}_{lt})} N_{lt}, \tag{24}$$

where $\bar{\omega}_{lt}$ is shorthand notation for $\bar{\omega}(P_{lt})$.

The model is set up such that an entrepreneur always wishes to fully disinvest their entire net worth to fund investment projects. Accordingly, one can calculate an entrepreneur's gross expected return on internal funds (ERIF) as the ratio of $P_{lt} f(\bar{\omega}_{lt}) i_{lt}$ (the expected income generated by capital production by an entrepreneur) to net worth n_{lt} (the amount of funds the entrepreneur places in capital production). Using equation (21), we write

$$ERIF_{lt} = \frac{P_{lt} f(\bar{\omega}_{lt}) i_{lt}}{n_{lt}} = \frac{P_{lt} f(\bar{\omega}_{lt})}{1 - P_{lt} g(\omega_{lt})}, \tag{25}$$

which is always greater than the return to external funds, owing to agency costs.

2.4.2 Budget constraint and consumption decision

Here, we must take into account the heterogeneity across entrepreneurs. Let's first consider the case of an entrepreneur that draws a period-t level of productivity $\omega_{jt} < \bar{\omega}_t$. The entrepreneur defaults on the loan contract and sees the CMF confiscates their entire output of investment goods $\omega_{jt} i_{jt}$. The entrepreneur thus has no income left to finance current consumption and no capital goods to carry into the next period.

Consider now the case of an entrepreneur that does not default ($\omega_{jt} > \bar{\omega}_t$). The entrepreneur produces $\omega_{jt} i_{jt}$ units of investment goods. Some of that, $(1 + r^k_t)(i_{jt} - n_{jt})$, goes back to the CMF to honour the debt agreement. What is left is allocated between (i) current-period consumption (c^E_{jt}) and (ii) capital carried into the future period (k^E_{jt+1}). Evidently, the choice of k^E_{jt+1} influences next-period net worth n_{jt+1}, which influences the expected

income next period F^E_{jt+1}.[8] Therefore, when making its decision about k^E_{jt+1} in period t, the entrepreneur takes into account the following $t+1$ budget constraint

$$\frac{c^E_{jt+1}}{P_{t+1}} + k^E_{jt+2} \leq i_{jt+1} f(\bar{\omega}_{jt+1}). \tag{26}$$

Updating the formulas for investment (21) and net worth (10) by one period in the future we can rewrite the above budget constraint as

$$\frac{c^E_{jt+1}}{P_{t+1}} + k^E_{jt+2} \leq (r_{t+1} k^E_{jt+1} + P_{t+1}(1-\delta) k^E_{jt+1}) \frac{f(\bar{\omega}_{t+1})}{1 - P_{t+1} g(\bar{\omega}_{t+1})}. \tag{27}$$

The solvent entrepreneur's problem is to maximize expected lifetime utility (9), subject to the sequence of budget constraints. Assuming an interior solution, this problem yields the following Euler equation (now including country subscript l):

$$P_{lt} = \beta \Gamma E_t \left\{ [r_{lt+1} + P_{lt+1}(1-\delta)] \underbrace{\frac{P_{lt+1} f(\bar{\omega}_{lt+1})}{1 - P_{lt+1} g(\bar{\omega}_{lt+1})}}_{\text{ERIF}_{lt+1}} \right\}. \tag{28}$$

This Euler equation has a natural interpretation. The left side reflects the cost incurred by the entrepreneur to increase k^E_{jt+1} by one unit. The right side shows the expected discounted benefit of increasing k^E_{jt+1}. Such an increase raises the entrepreneur's net worth next period by an amount given by the term in square brackets. This additional net worth will be entirely used to finance investment projects in $t+1$, which is why it is multiplied by the gross expected return on internal funds (displayed in equation (25)).

To complete this section, we derive the aggregate budget constraint of the entire group of entrepreneurs. Recall that entrepreneur j has expected net income (in period t) given by $i_{jt} f(\bar{\omega}_{jt})$. This takes into account (i) repayment of the loan to the CMF when the realized productivity turns out to be greater than $\bar{\omega}_{lt}$ and (ii) the possibility that the entrepreneur has a level of productivity lower than $\bar{\omega}_{lt}$, in which case, the loan is not repaid to the CMF and sees its output of investment goods confiscated by the CMF. Now let I_t denote aggregate "per entrepreneur" investment in the production of investment goods. With an infinite number of entrepreneurs and, given the linearity of the expected income formula above, the law of large numbers implies that we can interpret $I_t f(\bar{\omega}_t)$ as aggregate "per entrepreneur" net income in period t. At the end of the period, the group of entrepreneurs sell C^E_t / P_t units of capital back to the CMF to fund their period-t consumption, where C^E_{lt} denotes "per entrepreneur" consumption. Remaining units of investment goods are carried into the following period and

[8] The expected income in period $t+1$, denominated in units of $t+1$ investment goods, is $F^E_{jt+1}/P_{t+1} = i_{jt+1} f(\bar{\omega}_{jt+1})$. This takes into account (i) the repayment of the loan to the CMF when the realized productivity turns out to be greater than $\bar{\omega}_{jt+1}$ and (ii) the possibility that the entrepreneur has a level of productivity lower than $\bar{\omega}_{jt+1}$, in which case, the loan is not repaid to the CMF and sees its output of investment goods confiscated by the CMF.

constitute K^E_{t+1}, the "per entrepreneur" stock of capital at the beginning of period $t+1$. Then, aggregating over all the entrepreneurs' budget constraints yields

$$\frac{C^E_t}{P_t} + K^E_{t+1} \leq I_t f(\bar{\omega}_t). \tag{29}$$

Using the aggregate equivalent of equation (21) and aggregate "per entrepreneur" net worth, we can rewrite the above budget constraint as (now adding back the country subscript l)

$$\frac{C^E_{lt}}{P_{lt}} + K^E_{lt+1} \leq (r_{lt}K^E_{lt} + P_{lt}(1-\delta)K^E_{lt})\frac{f(\bar{\omega}_{lt})}{1 - P_{lt}g(\omega_{lt})}. \tag{30}$$

2.5 The representative capital mutual fund

The final component of our model is the intermediation sector, where there is a large number of identical and perfectly competitive capital mutual funds. All loanable funds in our model ultimately come from households who forward some of their savings to the representative CMF in return for investment goods. The CMF then lends to entrepreneurs these units of consumption goods received from households. We assume that all CMFs are risk neutral. Is this assumption appropriate, given that CMFs allocate household savings and that households are risk averse? It turns out that it is. First, note that there is no uncertainty over the length of the contracts between CMFs and entrepreneurs. Second, there is an infinitely large number of entrepreneurs and there is no aggregate uncertainty about the distribution of ω. This implies that CMFs face no uncertainty about the total quantity of investment goods they are going to get from the population of entrepreneurs. Hence, CMFs can guarantee households that they will receive I^h units of investment goods in exchange for PI^h units of consumption goods. Thus, we can think of households as being risk neutral in their willingness to loan funds.

We now describe all flows of consumption and investment goods going in and coming out of the financial intermediation sector.[9] We begin by accounting for the flow of consumption goods in country l. The items in the list below are arranged chronologically.

- Households pay $P_{lt}I^H_{lt}$ to CMFs to purchase investment goods. Investment goods will be delivered to households later in period t.
- CMFs pay $P_{lt}(1-\delta)K^E_{lt}$ to entrepreneurs when purchasing their undepreciated capital stock.
- CMFs lend $I_{lt} - N_{lt}$ to entrepreneurs as per their contracts. Aggregating up (21), we can write $I_{lt} - N_{lt} = P_{lt}g(\bar{\omega}_{lt})I_{lt}$.
- CMFs sell C^E_{lt} to entrepreneurs for their period t consumption.

[9] Recall that CMFs produce neither consumption nor investment goods.

The flow of consumption goods in country l implies that

$$\underbrace{P_{lt} I_{lt}^H}_{inflow} = \underbrace{P_{lt}(1-\delta)K_{lt}^E + P_{lt} g(\omega_{lt}) I_{lt} + C_{lt}^E}_{outflow}. \tag{31}$$

Let's now look at flows of investment goods in country l, again arranged chronologically.

- CMFs buy $(1-\delta)K_{lt}^E$ from entrepreneurs.
- A solvent entrepreneur j pays back $(1+r_t^k)(i_{jt} - n_{jt})$ to CMFs to honour its debt contract. Alternatively, CMFs get $(\omega_j - \mu)i_j$ from entrepreneur j when it defaults. In the aggregate, the law of large numbers implies that CMFs receive from the entire group of entrepreneurs $g(\bar{\omega}_{lt})I_{lt}$ units of investment goods.
- Households receive the I_{lt}^H units of investment goods they paid for earlier in the period.
- Entrepreneurs pay C_{lt}^E / P_{lt} for the purchase of C_{lt}^E units of consumption goods.

Therefore, it must be the case that

$$\underbrace{(1-\delta)K_{lt}^E + g(\bar{\omega}_{lt})I_{lt} + \frac{C_{lt}^E}{P_{lt}}}_{inflow} = \underbrace{I_{lt}^H}_{outflow}. \tag{32}$$

Therefore, total profits (denominated in consumption goods) earned by the financial intermediaries in country l (inflows less outflows) are $\Pi_{lt}^{CMF} =$

$$\begin{array}{c} \left\{ P_{lt} I_{lt}^H + P_{lt} \left[(1-\delta)K_{lt}^E + g(\bar{\omega}_{lt})I_{lt} + \frac{C_{lt}^E}{P_{lt}} \right] \right\} \\ - \left\{ P_{lt}(1-\delta)K_{lt}^E + P_{lt} g(\bar{\omega}_{lt}) I_{lt} + C_{lt}^E + P_{lt}[I_{lt}^H] \right\} \end{array}, \tag{33}$$

which are equal to zero as implied by (31) and (32).

2.6 Shocks

The productivity shocks driving the TFP of intermediate goods producers are assumed to follow a stationary first-order vector-autoregressive process given by

$$\begin{bmatrix} \ln Z_{1t} \\ \ln Z_{2t} \end{bmatrix} = \begin{bmatrix} \rho_z & \rho_s \\ \rho_s & \rho_z \end{bmatrix} \begin{bmatrix} \ln Z_{1t-1} \\ \ln Z_{2t-1} \end{bmatrix} + \epsilon_{z,t} \tag{34}$$

$$E(\epsilon_{z,t}\epsilon_{z,t}') = \Sigma_z, \tag{35}$$

where the vector of innovations $\epsilon_{z,t} = [\varepsilon_{z_1,t} \quad \varepsilon_{z_2,t}]'$ is realized at the beginning of period t (before any decisions are made). Innovations are normally distributed and are independent over time. Parameters ρ_z and ρ_s govern the degrees of persistence and international spillovers of the shocks, respectively. Σ_z denotes the variance-covariance matrix of ϵ_z.

2.7 Market-clearing conditions and other variables

The total amount of intermediate goods produced in period t in country 1 is allocated as follows

$$Y_{1t} = a_{1t} + a_{2t}, \tag{36}$$

where a_{1t} is the number of units of good a used in the production of country 1's final good, and a_{2t} is the number of units exported to country 2, where it is used in the production of that country's final good. In the same way, country 2's output of good b is allocated as

$$Y_{2t} = b_{1t} + b_{2t}, \tag{37}$$

where b_{2t} is the number of units of good b used in the production of country 2's final good, and b_{1t} is the number of units exported to country 1, where it is used in the production of that country's final good.

The variable H_{lt}, which appears in the representative household's utility function and the representative intermediate good producer's production function, represents both total household labour supplied and total demand for household-type labour by intermediate firms in country l, thus clearing the labour market.

For capital markets to clear, capital supply $K_{lt}^E + K_{lt}^H$ must equal the total capital demanded by the intermediate firm K_{lt}

$$K_{lt} = K_{lt}^E + K_{lt}^H. \tag{38}$$

The representative household's capital accumulation, equation (6), and the overall entrepreneurial budget constraint, equation (29), imply the accumulation equation

$$K_{lt+1}^H + K_{lt+1}^E = (1-\delta)K_{lt}^H + I_{lt}^H + f(\bar{\omega}_{lt})I_{lt} - \frac{C_{lt}^E}{P_{lt}}. \tag{39}$$

Substituting out I_{lt}^H using equation (32) yields

$$K_{lt+1}^H + K_{lt+1}^E = (1-\delta)K_{lt}^H + (1-\delta)K_{lt}^E + [g(\bar{\omega}_{lt}) + f(\bar{\omega}_{lt})]I_{lt} + \frac{C_{lt}^E}{P_{lt}} - \frac{C_{lt}^E}{P_{lt}}. \tag{40}$$

Using equations (38) and (16) gives us the aggregate capital accumulation equation[10]

$$K_{lt+1} = (1-\delta)K_{lt} + [1 - \Phi(\bar{\omega}_{lt})\mu]I_{lt}. \tag{41}$$

As for the market-clearing condition for final goods, we have

$$C_{1t}^H + C_{1t}^E + I_{1t} = G(a_{1t}, b_{1t}), \qquad C_{2t}^H + C_{2t}^E + I_{2t} = G(b_{2t}, a_{2t}). \tag{42}$$

We assume complete markets in state-contingent claims available to the households to diversify country-specific risks. These assets are traded exclusively between domestic and foreign households. Market clearing requires that the following condition holds:

$$D_1(s^t, s_{t+1}) + D_2(s^t, s_{t+1}) = 0 \quad \text{for all } s_{t+1}. \tag{43}$$

When these assets are available, households perfectly diversify country-specific risk, and the equilibrium allocations are such that in all states of the world, the utility gained from an additional unit of good a in country 1 is exactly the same as the utility gained in country 2. The same holds for good b.

There are some key variables that we have not yet defined. Unless otherwise indicated, all of our consumption statistics are calculated using aggregate consumption measured as $C_{lt} = C_{lt}^H + C_{lt}^E$.

A country's terms of trade (TOT) are defined as the price of that country's imports relative to that of its exports. When we refer to the terms of trade, we are implicitly referring to country 1's terms of trade, which is given by q_{2t}/q_{1t}. Using the representative final good producer's first-order conditions, we find

$$TOT_t = \frac{q_{2t}}{q_{1t}} = \frac{\partial G_1(a_{1t}, b_{1t})/\partial b_{1t}}{\partial G_1(a_{1t}, b_{1t})/\partial a_{1t}} = \frac{1-\kappa}{\kappa}\left(\frac{a_{1t}}{b_{1t}}\right)^{\frac{1}{\sigma}}. \tag{44}$$

Gross domestic product in country 1 in units of the final good is $GDP_{1t} = q_{1t}Y_{1t}$, while for country 2, we have $GDP_{2t} = q_{2t}^* Y_{2t}$.

Country 1's ratio of net exports to GDP is calculated as

$$NX_{1t} = \frac{q_{1t}a_{2t} - q_{2t}b_{1t}}{GDP_{1t}} = \frac{a_{2t} - TOT_t b_{1t}}{Y_{1t}}. \tag{45}$$

[10]The aggregate capital accumulation equation suggests that our model with financial frictions resembles a model with investment adjustment costs. That is indeed the case. As pointed out by Carlstrom and Fuerst (1997) the financial-frictions framework, as presented in our benchmark, provides a micro-founded alternative to investment adjustment costs through the short-term impact financial frictions have on investment production. The results of a model with investment adjustment costs and without the financial-frictions framework outlined above is available upon request.

Following Raffo (2008), we also look at the trade balance at constant prices (prices are set to their steady-state values). For the home country we have

$$NXQTY_{1t} = \frac{a_{2t} - \bar{TOT} b_{1t}}{Y_{1t}}, \tag{46}$$

where $\bar{TOT}$ denotes the steady-state value of TOT.

3 Benchmark Model Solution and Parameter Values

We perform a second-order approximation around a symmetric deterministic steady-state equilibrium where both countries' net exports equal zero. The parameter values we select are commonly used in both agency costs and international real business-cycle literature. Just like BKK and their many offsprings, we have in mind a model where one country represents the United States, the other represents the euro area and a period is one quarter of a year. Table 1 summarizes the parameter values we use in our benchmark model. The model is simulated for 100,000 periods and the first 100 periods are discarded. The simulated data are then passed through the Hodrick-Prescott filter (with a smoothing parameter of 1,600) before calculating the statistical moments listed in Tables 2 and 3. We now explain how we assign values to the parameters in our international business-cycle model.

3.1 Household preferences

The value of the representative household's discount factor is $\beta = 0.985$. The household's coefficient of risk aversion is set equal to $\gamma = 2$. The values for β and γ are well within the acceptable range found in the literature. The parameter ν governs the curvature of the household's preferences. When preferences are of the GHH type ($\eta = 0$), the labour supply elasticity is given by $1/(\nu - 1)$. Jaimovich and Rebelo (2009) set $\nu = 1.4$, Letendre and Luo (2007) use 1.7, while Johri, Letendre and Luo (2011) use 3. Raffo (2010) points out that when preferences are of the GHH type, $\nu = 1.64$ implies the same Frisch elasticity of labour supply (1.5) as considered by BKK (1994). We set $\nu = 1.63$ but also consider a higher value in our sensitivity analysis. Parameter η influences the intensity of the wealth effect on household labour supply. GHH preferences are seen more and more in the international macro literature. An early example is Correia, Neves and Rebelo (1995) and a recent example is Mandelman et al. (2011). In the spirit of Jaimovich and Rebelo (2009), we select a small value for η so that we do not entirely shut down the income effect on labour supply as GHH preferences do. We use $\eta = 0.10$ but also consider $\eta = 1$. Parameter ψ is set to ensure that the representative household spends 30% of its time working in the steady state.

3.2 External shock process

Parameter ρ_z represents the degree of persistence of productivity shocks. For quarterly models, estimated values for this parameter range from 0.906 (Backus, Kehoe and Kydland, 1992) all the way up to unity (e.g., Baxter and Crucini, 1995). We pick the midpoint of this range and use $\rho_z = 0.95$ in our benchmark case. Given that we want to study the model's ability to produce positive international co-movements in the RPI, we do not allow for any connections between shocks across the two countries in our benchmark case. Accordingly, we set $\rho_s = 0$ and set the correlation of ε_{z_1} and ε_{z_2} to zero. We consider other values for ρ_z, ρ_s and $correl(\varepsilon_{z_1}, \varepsilon_{z_2})$ in our sensitivity analysis. The standard deviation of ε_{z_1} and ε_{z_2} is set to match output volatility in the United States.

3.3 Intermediate goods

We set the capital share to $\alpha_K = 1/3$. We preserve a constant returns-to-scale set-up by having $\alpha_H = 1 - \alpha_K$.

3.4 Final good production

Production of the final good requires both domestically produced and imported intermediate goods. Recall that σ denotes the elasticity of substitution between domestic and imported intermediate goods and that κ determines home bias. Values of σ employed in the literature vary greatly. For example, BKK (1994), Chari, Kehoe and McGrattan (2002) and Raffo (2008) use 1.5. Heathcote and Perri (2002) use time-series data and get an estimated elasticity of 0.9. Mandelman et al. (2011) use 0.62. Others, such as Hooper, Johnson and Marquez (2000), estimate a short-run trade elasticity in the United States of around 0.6 and less for other G7 countries. Even short-run trade elasticities as low as 0.22, as used in Taylor (1993), have been suggested, implying that traded goods are highly complementary. Corsetti, Dedola and Leduc (2007), Benigno and Thoenisssen (2008) and Raffo (2010) all allow for an elasticity of substitution at or below 0.5.[11] In line with current research, we use an elasticity of substitution $\sigma = 0.5$. We also use Heathcote and Perri's (2002) estimated elasticity in our sensitivity analysis. As for home bias, we set κ such that the share of imports to total intermediate goods output (denoted im) is always equal to 0.15, as in BKK (1994) among others. With import share im, and the value assigned to σ this implies a home bias of

$$\kappa = \left(1 + \left(\frac{1 - im}{im}\right)^{(1/\sigma)}\right)^{-1}, \tag{47}$$

[11] This lack of consensus on the appropriate value of σ led Bodenstein (2011) to publish an article listing the consequences of varying this elasticity.

which is the same for both countries.

3.5 Stochastic entrepreneurial productivity

Recall that an entrepreneur is given a productivity level ω drawn from a distribution $\phi(\omega)$. These idiosyncratic productivities must be non-negative and could range in value from 0 to ∞. The benchmark model assumes that the distribution of entrepreneurial productivity is a lognormal distribution with a mean of 1. Accordingly, we use

$$\phi(\omega) = \frac{1}{\omega\sqrt{2\pi\sigma_\omega^2}} e^{-\frac{(ln(\omega)-\mu_\omega)}{2\sigma_\omega^2}}, \qquad \Phi(\omega) = \frac{1}{2} + \frac{1}{2} ERF\left[\frac{ln(\omega)-\mu_\omega}{\sqrt{2\sigma_\omega^2}}\right], \tag{48}$$

where μ_ω and σ_ω refer, respectively, to the mean and standard deviation of the variable's natural logarithm.

When an entrepreneur's realized productivity is below the threshold $\bar{\omega}$ it defaults on their contract, which prompts monitoring by the CMF. At the aggregate level, the monitoring costs incurred by the CMF is equal to $\mu Pi\Phi(\bar{\omega})$. These losses can be anything from legal fees to lost sales. Given the broad interpretation of what could be included in these losses, the possible range for the monitoring cost μ is quite broad. Carlstrom and Fuerst (1997) give a possible range for the value of μ from as low as 0.2 to as high as 0.36. For ease of comparison, we adopt the same monitoring cost as CF, setting μ equal to 0.25.

We choose the standard deviation of entrepreneurial productivity σ_ω to match the 0.974 quarterly bankruptcy rate as reported by Fisher (1999). We follow CF and set $1/\Gamma$ equal to the return on internal investment. Notice that when there are agency costs, the internal rate of return is always greater than the rate of return on external funds, owing to the risk premium charged on borrowed funds. If the discount factor Γ is too high, the entrepreneur continues to accumulate capital until the point where it is self-financed, and there would be no agency costs in the steady state. If the discount rate is too low, the entrepreneur heavily discounts future consumption, opting for current consumption, in which case, the entrepreneur chooses to hold no capital in the steady state. Therefore, in order for there to be a stable equilibrium, the internal rate of return must equal $1/\Gamma$ or

$$P_l \frac{f(\bar{\omega})}{1 - P_l g(\bar{\omega})} = \frac{1}{\Gamma}. \tag{49}$$

Accordingly, we set $\Gamma = 0.947$. This value implies an entrepreneurial discount factor of $\beta\Gamma = 0.937$. The steady-state relative price of capital $\bar{P}$ is equal to 1.024, with the entrepreneur's share of investment production $f(\bar{\omega}) = 0.39$.

4 Results–Benchmark Model

4.1 Business-cycle statistics

Table 2 contains the statistical moments produced by our benchmark model. The Data column reproduces the moments reported in BKK (1993). That column also displays the statistics pertaining to the terms of trade and net exports reported in Raffo (2008) (indicated with a superscript R). Finally, we calculated statistics related to the RPI using the data described in the Appendix. In the Data column, the statistics we calculated are identified by a superscript LW. We report two numbers for the relative standard deviation of the RPI. Both are calculated using U.S. data. When using quality-adjusted data to calculate the RPI, its relative standard deviation is 0.39. When no quality adjustments are made, the relative standard deviation of the RPI is 0.15. Since we do not have quality-adjusted data for our aggregate of the euro area, we use unadjusted data to calculate the correlation between the RPI-United States and RPI-euro area. All statistics reported are calculated using HP filtered data (smoothing parameter equal to 1600).

Our model matches the standard deviation of GDP exactly, since the calibration of the variance of technology shocks targeted that moment. The first autocorrelation of GDP is large and positive (0.76 vs 0.86 in the data). The "within country" moments are broadly consistent with the data. Consumption and hours worked are less volatile than GDP, while investment is significantly more variable than GDP. Those three variables are very highly correlated with GDP. The entirely endogenous RPI appearing in the benchmark model is a little less variable (relative to GDP) as the quality-adjusted RPI in the United States (0.30 vs 0.39).

The model is also doing a good job at producing realistic international business cycles. TOT are highly volatile. Their relative standard deviation (1.74) falls in the range of estimates reported in the literature (1.12 in Raffo and 1.92 in BKK). The same holds true for net exports. The correlation of net exports with GDP (-0.50) is in the range reported in the literature (-0.51 in Raffo and -0.37 in BKK), while net exports at constant prices are not as countercyclical as in the data (Raffo reports a correlation with GDP of -0.41, and in our model it is -0.15). All cross-country correlations are positive but do not numerically match the corresponding numbers in the data. It is true that the cross-country correlations of investment and consumption are rather low. However, one has to remember that, unlike what is commonly done in the literature, productivity shocks are not correlated across countries in our model.

As is well known, the BKK model struggles to replicate some key empirical regularities: most notably, they fail to replicate the positive correlation of output, consumption, labour and investment across countries, as well as the high volatility of the TOT. A number of extensions have been proposed to address these shortcomings. A recent example is Raffo (2008), who shows that using GHH preferences enables the model to produce a positive

cross-country correlation of labour. A detailed sensitivity analysis focusing on international correlations and the volatility of the TOT can be found in Heathcote and Perri (2002). They show that lowering the elasticity of substitution between intermediate goods (σ) as well as lowering the degree of spillovers in productivity shocks raises the international correlations while also moderately increasing the variance of the TOT. Our paper contributes to that strand of the international business-cycle literature by showing how financial frictions à la Carlstrom and Fuerst help address (to some extent) some of the glaring shortcomings of the canonical BKK model.

We document the effect of financial frictions by comparing our benchmark model against a special case of the model where financial frictions have been removed. The moments implied by the latter model are found in Table 2 in the column titled No Fin. Frictions.[12] Notice how the cross-country correlations all increase a little and how the standard deviation of the TOT also increases when financial frictions are added to the model.[13] While these changes are not spectacularly large, notice that they occur in a set-up where the standard deviation of the RPI relative to that of output in the model is about three-quarters of its quality-adjusted counterpart in our U.S. data (0.30 vs 0.39). Hence, the model has potential to do better.

A central contribution of our paper is to propose a model where the cross-country correlation of the RPI is determined entirely endogenously. As a result of international trade in intermediate goods, the model delivers a small positive cross-country correlation for the RPI, which is close to what is seen in U.S./euro-area data. Similar to Dmitriev and Roberts (2012), our model relies on a low wealth effect on labour supply in order to help bolster cross-country correlations. However, unlike Dmitriev and Roberts (2012), our model does not rely on cross-country correlations in neutral technology or high levels of habit formation in consumption in order to generate positive cross-country correlations in investment. Furthermore, with a low elasticity of labour supply ($\eta = 0.1$) along with a low elasticity of substitution between domestic- and foreign-produced intermediates ($\sigma = 0.5$), our model is capable of generating positive cross-country correlations in hours worked. If the wealth effect on labour supply an the elasticity of substitution between domestic- and foreign-produced intermediate goods were increased simultaneously, as is the case under Heathcote and Perri's (2002) choice of calibration, cross-country correlations in hours worked would be reduced significantly. In the next section, we use impulse-response functions to explain how the model generates this positive correlation.

[12]The only difference between the benchmark model and the no-financial-frictions model is that the latter has no entrepreneurs or CMFs. Therefore, future capital can be increased by one unit simply by reducing consumption by one unit. We simulate that model using the very same parameter values as in our benchmark model.

[13]Most other moments remain basically unchanged except the correlation of GDP with net export at constant prices, which unfortunately rises.

4.2 Impulse-response functions

The parameter values used are exactly the same as those in our benchmark case (see Table 1). In all figures discussed below, the variables are represented in percentage deviations from the steady state and have not been filtered in any way. The economy is in the steady state in period 0 and a shock hits one of the countries in period 1.

Figures 1-3 plot the responses to a 1% unexpected increase in the home country's total factor productivity (Z_1) in period 1. The solid line corresponds to the benchmark model and the dotted line to the no-financial-frictions model (NFF henceforth). Recall that our stochastic process is such that the first-order autocorrelation of Z_1 is 0.95. Therefore, total factor productivity in country 1 remains above its steady-state value for several periods (half-life of 14 periods). Output, hours worked, investment and consumption in both countries increase in response to a shock in country 1 and have a prominent hump shape.[14] The shape of these responses is not surprising in light of the work of Carlstrom and Fuerst (1997).

Figure 1 shows that the response of investment in the home country is slightly weaker when financial frictions are present. Interestingly, the sign of the initial response of investment in the foreign country differs in the two models (Figure 2). We witness a small positive response in our benchmark model and a slightly negative response in the NFF model. Figure 3 shows the responses of the terms of trade and net exports. The initial response of the home country terms of trade is noticeably larger in the benchmark model than in the NFF model. As the discussion below makes clear, the higher volatility of the terms of trade in the benchmark model and the response of investment are closely related. We now provide some economic intuition connecting the model to the impulse responses.

Recall that productivity shock Z_1 appears in the production function of intermediate goods producers in country 1 and nowhere else. These producers use capital and labour to produce good a. A positive shock to Z_1 increases the marginal product of capital and labour, which drives up the demand for those factors of production. Hence, wages and rents on labour and capital services increase. Since entrepreneurs supply capital to the intermediate goods producers, the increased return on capital generates an immediate increase in the entrepreneurs' net worth (see equation (10)). Since the bulk of the entrepreneurs' net worth is determined by the value of their capital stock (a state variable), the overall increase in net worth is relatively small in the period of the shock. Figure 1 shows that net worth increases by about 0.5% in period 1, which is much smaller than the peak increase in net worth (about 4% in period 3).

Responding to an increase in the return to physical capital, households desire to acquire more capital goods. The slow response of net worth implies that entrepreneurs who want to increase the size of their projects need more external financing. As a result, agency costs and, hence, the price of investment increase (see Figure 1). Since the return to internal funds

[14]The observation that GDP responds in a hump-shaped manner to a temporary productivity shock goes at least as far back as Cogley and Nason (1995).

(25) is increasing in P, entrepreneurs respond to the increased demand for capital goods by significantly reducing their consumption (it falls 25% below its level in the steady state) in response to the TFP shock in order to bolster internal funds. Consequently, entrepreneurial net worth rises importantly in period 2. As entrepreneurial wealth increases, entrepreneurs can respond to the higher demand for capital while relying less on external financing. This drives down both agency costs and the RPI in period 2, making for a short-lived rise in the relative price of investment.

One may wonder why I_2 increases in the model with financial frictions given that the price of investment P_2 increases in response to the shock, whereas that very same price is constant in the model without financial frictions. The answer lies in the response of another relative price: the TOT. Given the increase in P_1, the home country faces higher costs of producing investment goods in our model than in the NFF model. Hence, it desires to invest less. Therefore, country 1 needs fewer units of final goods, which means it requires fewer units of its own intermediate good. Hence, a larger quantity of good a ends up being supplied to the world market. This leads to a sharper fall in the price of that good and, hence, a more important increase in country 1's terms of trade (as Figure 3 makes clear). Figures 1 and 3 show a spike in the TOT at the very same time that P_1 spikes.

When the price of good a plummets, country 2 sees an opportunity to purchase a greater quantity of it, which can then be bundled with its own intermediate good to raise the quantity of final goods produced in country 2. Being consumption smoothers, households in country 2 consume some of that additional quantity of final goods and invest some of it in physical capital to raise future consumption. Raising the amount of final goods in country 2 requires that intermediate producers increase their output of good b since goods a and b are not perfect substitutes. Given that Z_2 does not change, more output of good b requires more labour and capital. The stronger demand for factors of production raises wage and rental rates. Consequently, the wealth of country 2 entrepreneurs increases but not enough to match the increase in the size of their projects. Thus, they must rely more heavily on external funding which raises agency costs in country 2 as well as P_2 (see Figure 2).

Overall, our theoretical setup suggests that agency costs can be transmitted from one country to another through trade in goods. This endogenous transmission channel produces a positive cross-country correlation in the RPI.

5 Alternative Models

5.1 Model with an exogenous RPI (IST model)

In this section, we look at a model where the RPI is exclusively driven by investment-specific technology (IST) shocks. We consider this model for two reasons. First, to provide a direct

comparison of a model where the RPI is entirely endogenous (our benchmark model) to a model where it is entirely exogenous. Our second objective is to contribute to the debate about the role played by IST shocks in international business-cycle models.

We add IST shocks (denoted V_{1t} and V_{2t}) to our model without financial frictions. That involves replacing the resource constraints shown in equation (42) with $C_{1t}^H + C_{1t}^E + \frac{I_{1t}}{V_{1t}} = G(a_{1t}, b_{1t})$ and $C_{2t}^H + C_{2t}^E + \frac{I_{2t}}{V_{2t}} = G(b_{2t}, a_{2t})$ and adding to the model the bivariate vector-autoregressive process

$$\begin{bmatrix} \ln V_{1t} \\ \ln V_{2t} \end{bmatrix} = \begin{bmatrix} \rho_v & 0 \\ 0 & \rho_v \end{bmatrix} \begin{bmatrix} \ln V_{1t-1} \\ \ln V_{2t-1} \end{bmatrix} + \epsilon_t, \tag{50}$$

$$E(\epsilon_t \epsilon_t') = \Sigma \tag{51}$$

where the vector of innovations is now $\epsilon_t = |\epsilon_{v1t}, \epsilon_{v2t}|'$. The bivariate autoregression above is estimated using U.S./euro-area data to determine the degree of spillovers and persistence of the HP-filtered RPI in both countries.[15] With estimated values of 0.84 and 0.72 for the persistence of technology in the United States and euro area, respectively, we chose a value for the persistence parameter ρ_v of 0.78, the average of the two estimates. Off-diagonal elements were found to be not statistically different from zero. The standard deviations of ϵ_{v1t} and ϵ_{v2t} and their correlation are calibrated to ensure that the model with IST shocks, is consistent with the relative standard deviation of the quality-adjusted RPI (0.39) and the cross-country correlation of RPI reported in Table 2. Finally, since the volatility of GDP increases when we include IST shocks, we lower the standard deviation of TFP shocks to insure that the model produces a standard deviation of GDP equal to 1.92.[16] All other parameters retain the values reported in Table 1.

Focusing exclusively on the moments produced by the benchmark and IST models (Table 2), one could argue that the overall fit of the IST model is just as good as that of our benchmark model. On the one hand, the benchmark model generates more variance in the terms of trade and produces cross-country correlations of GDP and investment that are significantly closer to the data. On the other hand, the IST model produces a more countercyclical real trade balance (NXQTY) and a cross-country correlation of hours worked that is closer to the data. Both models produce realistic variance in the RPI and realistic cross-country correlations of the RPI. Given that the RPI is entirely endogenous in the benchmark model, we conclude that it dominates the IST model.

A question that has been debated in the international business-cycle literature is the importance of IST shocks. Raffo (2010), using an ad hoc calibration of the IST shocks process finds that these shocks "resolve" the so-called quantity and price anomalies first underlined by BKK. Mandelman et al. (2011) estimate the process for IST shocks using RPI data and do not find that IST shocks resolve the quantity and price anomalies. The moments

[15] We thank a referee for suggesting this approach.

[16] Specifically, we use $SD(\epsilon_{v1}) = SD(\epsilon_{v2}) = \sqrt{0.00004}$, $SD(\epsilon_{z1}) = SD(\epsilon_{z2}) = \sqrt{0.0000122}$ and $correl(\epsilon_{v1}, \epsilon_{v2}) = 0.12$.

reported in Table 2 show that adding IST shocks to our model without financial frictions somewhat improves the volatility of the TOT and their correlation with GDP. However, the cross-country correlations of GDP and investment worsen when we add IST shocks. Overall, it's far from clear that IST shocks help international business-cycle models match the data better. Our benchmark model fits at least as well as the IST model and has the superior feature that changes in RPI are actually explained by the model.

5.2 Model with risk shocks

Christiano, Motto and Rostagno (2014) find that risk shocks play a significant role in explaining the U.S. business cycle. Our analysis of risk shocks contributes to the literature by providing a detailed account of the implications that risk shocks have in an international environment. Risk shocks are incorporated into our benchmark model by making the variance of the distribution of entrepreneurial productivity (ω) a random variable. A positive risk shock in country i leads to a dispersion in the cross-sectional distribution of entrepreneurial productivity in that country. This effectively increases the level of uncertainty for lenders, as the range of possible values for ω increases.

Risk shocks follow a stationary first-order vector autoregressive process given by

$$\begin{bmatrix} \ln(\sigma_{\omega_1,t}/\sigma_\omega) \\ \ln(\sigma_{\omega_2,t}/\sigma_\omega) \end{bmatrix} = \begin{bmatrix} \rho_\sigma & 0 \\ 0 & \rho_\sigma \end{bmatrix} \begin{bmatrix} \ln(\sigma_{\omega_1,t-1}/\sigma_\omega) \\ \ln(\sigma_{\omega_2,t-1}/\sigma_\omega) \end{bmatrix} + \epsilon_{\sigma_\omega,t}, \tag{52}$$

$$E(\epsilon_{\sigma_\omega,t}\epsilon'_{\sigma_\omega,t}) = \Sigma_\omega \tag{53}$$

where the vector of innovations $\epsilon_{\sigma_\omega,t} = [\varepsilon_{\sigma_{\omega_1},t} \;\; \varepsilon_{\sigma_{\omega_2},t}]'$ is realized at the beginning of period t (before any decisions are made). Innovations are normally distributed and are independent over time. The parameter ρ_σ governs the degree of persistence of risk shocks, while σ_ω denotes the steady-state value for the standard deviation of $log(\omega)$. Σ_ω denotes the variance-covariance matrix of $\epsilon_{\sigma_\omega,t}$.

Risk shocks are calibrated using data on the spread/risk premium between Baa-rated corporate bond rates and 10-year-ahead U.S. government bond rates, measured in levels. We use these data over the period from 1985Q1 to 2015Q1 to calculate a risk premium. We then HP-filtered that risk premium series and calculated its first-order autocorrelation (0.77) and variance (0.5). Our model does not produce much endogenous persistence in the risk premium paid by the entrepreneurs, so we set $\rho_\sigma = 0.99$. The variance of $\varepsilon_{\sigma_{\omega_1},t}$ was set to 0.000145 to match the variance of the risk premium series we calculated. We want to study the model's ability to produce positive international co-movements in the RPI; hence, we do not allow for any correlations, or spillovers in risk shocks across countries. All other parameters are set as in the benchmark model.

We begin our analysis of risk shocks by looking at impulse-response functions. Figures 4 to

6 plot responses to a 1% unexpected increase in the standard deviation of $log(\omega)$ in the home country in period 1. Recall that a positive risk shock leads to a spread in the distribution of entrepreneurial productivity. This leads to a rise in the productivity threshold $\bar{\omega}$ separating those that declare bankruptcy from those that choose to continue operating. The increase in this threshold leads to a rise in the proportion of entrepreneurs declaring bankruptcy. With the subsequent rise in agency costs, the RPI increases in the home country (see Figure 4). Consequently we see a drop in investment, followed by a decline in consumption and output in the home country. As with a technology shock, there is a surge in the quantity of the home country's intermediate goods on the global market leading to a deterioration of the home country's terms of trade (see Figure 6). This leads to a rise in investment, output, consumption and hours worked in the foreign country as they take advantage of the declining price of the home country's intermediate goods. The rise in investment in the foreign country gives rise to agency costs leading to an increase in the RPI. As with a technology shock, trade in intermediate goods propagates a spike in the home country RPI to the foreign country RPI. However, unlike technology shocks, risk shocks produce responses in GDP, consumption, hours worked and investment that are of opposite signs across countries.

The last column in Table 2 displays the moments generated by the risk-shocks model. It is very clear that risk-shocks of the size we include in our model do very little when compared with technology shocks. For all practical purposes, the numbers implied by the risk shocks model are identical to those implied by the benchmark model. In order to see which of the moments are most influenced by risk shocks, we run the model once more after multiplying the variance of risk shocks by 100. The results are reported in the first column of numbers in Table 3. Given our discussion of impulse responses above, it is not surprising to see that risk shocks have their most significant impacts on the variance of the RPI, on the terms of trade and on cross-country correlations, which all become smaller (except that of the RPI). Given the high significance placed by Christiano, Motto and Rostago (2014) on risk shocks in generating realistic business cycles, this presents a challenge to the current line of research.

Given the relative importance of risk shocks in the closed-economy model of Christiano, Motto and Rostago (2014), the lack of importance in our open-economy model is intriguing. This result, however, appears to be due to our decision to separate the entrepreneurs' consumption/savings decisions from those of households. As a consequence, a risk premium shock causes entrepreneurs to forgo consumption in order to bolster their net worth and decrease their reliance on borrowed funds. As entrepreneurs become more self-reliant (owing to increased net worth), the risk premium charged on borrowed funds decreases. Thus, the added flexibility of separating the entrepreneur's consumption decision from that of households causes the entrepreneur's net worth to respond quickly to a risk shock. For this reason, the increase in the risk premium charged on borrowed funds is relatively short-lived and contributes very little to the volatility of output, consumption and investment. When household and entrepreneurial consumption decisions are integrated, as is the case in Christiano, Motto and Rostago (2014), entrepreneurial net worth increases only gradually. This prolongs the lifespan of the risk shock on the real economy. An interesting result of our decision to separate household consumption from entrepreneurial consumption is the decline in aggregate consumption that results from a positive risk shock. The entrepreneur's decision to reduce

consumption to bolster net worth parallels the decline in consumption observed in the data. This occurs without sticky prices or sticky wages, which are required by Christiano, Motto and Rostago (2014) to match the positive correlation in consumption investment observed in the data.

6 Sensitivity Analysis

As discussed in Section 4, the addition of financial frictions in the form of agency costs into an otherwise canonical two-country, two-good international real-business cycle model has three key implications. First, the endogenous movements in the relative price of investment resulting from the presence of agency costs are empirically plausible. The variability of the relative price of investment is about 75% of its counterpart in U.S. data. The benchmark model produces a small positive cross-country correlation in the relative price of investment, which is just a little higher than what is measured in U.S./euro-area data. Second, financial frictions lead to higher volatility in the terms of trade while leaving the variance of net exports constant. Third, financial frictions lead to higher cross-country correlations in output, consumption, investment and hours worked. The latter two results improve upon the shortcomings of the canonical BKK model.

In this section, we analyze the sensitivity of our key results to changes in six parameters. We proceed in two ways. First, we show how the moments shown in Table 2 change when we vary parameters. Second, figures 7 to 10 display the sensitivity of cross-country correlations in output, consumption, investment and hours worked to four key parameters.[17] Each graph contains four lines. The solid line corresponds to the benchmark model, the dashed line corresponds to the model with risk shocks, the dotted line corresponds to the model with no financial frictions and the dot-dashed line corresponds to the IST model.

The household utility function we are using allows us to control the strength of the wealth effect on households' labour supply decisions. In our benchmark calibration, this wealth effect is modest ($\eta = 0.1$). Table 3 displays the moments implied by the benchmark model when the wealth effect is at its fullest ($\eta = 1$), effectively reverting to a KPR utility function. The volatility of the relative price of investment barely changes. The same holds for its cross-country correlation. The TOT are still highly variable. The cross-country correlations of GDP, consumption, and investment change very little. As expected, changing the labour supply wealth elasticity leads to significant changes in the volatility and the cross-country correlation of hours.

The parameter ν determines the labour supply elasticity. We test our results by raising ν from 1.64 to 3. The moments reported in Table 3 (column $\nu = 3$) are very similar to those observed when raising η to unity.

[17] We thank a referee for suggesting this exercise.

Next, we increase the elasticity of substitution σ from 0.5 to 0.9 (value estimated by Heathcote and Perri, 2002). The moments in Table 3 (column $\sigma = 0.9$) show that the volatility of the relative price of investment falls only marginally, while its cross-country correlation increases marginally. Figure 7 shows how cross-country correlations vary with σ. Increasing the elasticity of substitution leads to declines in cross-country correlations for GDP, investment and hours worked with an increase in the cross-country correlation of consumption. Notice how the correlations produced by the benchmark model (solid line) are never smaller than those produced by the other three models.

The final three sensitivity tests concern parameters appearing in the stochastic process for technology shocks. Not surprisingly, when we increase the cross-country correlation of productivity shocks, all cross-country correlations increase as shown in Figure 8. The relative standard deviation of the relative price of investment basically remains unchanged (0.29 vs 0.30) when the cross-country correlation of productivity shocks increases from 0 to 0.30. Figure 9 varies the technology spillover parameter ρ_s, while Figure 10 varies the persistence parameter ρ_z. In all three figures, the correlations produced by our model with financial frictions are greater than those produced by the other three models. The last column in Table 3 shows the moments produced by the benchmark model when we adopt the stochastic process for technology shocks estimated by Heathcote and Perri (2002). Here, $\rho_z = 0.97$, $\rho_s = 0.025$, and the cross-country correlation of technology shocks is 0.29. This combination of changes lowers the volatility of the relative price of investment marginally from 0.30 to 0.24 and increases its cross-country correlation by only a trivial amount (0.26 vs 0.25).

Overall, the results reported in Table 3 and in figures 7 to 10 demonstrate the robustness of our key results to parameter changes.

7 Conclusion

The effects agency costs have on economic aggregates in a closed economy have been well established (early examples are Bernanke and Gertler, 1989, and Carlstrom and Fuerst, 1997). However, little research has been done on the effects of agency costs in the context of international business-cycle models. We contribute to the international business-cycle literature by adding a financial sector in each country of a two-country, two-good BKK-style model. Our add-on is inspired by the work of Carlstrom and Fuerst (1997).

Our main finding concerns the dynamics of the relative price of investment. In our benchmark model, its variance, as well as its cross-country correlation, are comparable to the data. It is important to note that our model produces fluctuations and positive international co-movements in the RPI in an entirely endogenous fashion. Since its conception, IST has been identified exclusively by the inverse of the RPI. Given that our benchmark model generates positive co-movements in the RPI across countries endogenously, our model adds

to the work of Miyamoto and Nguyen (2013) by proposing an additional way that measured technology (in this case IST) moves together across countries through international trade. We show that this positive international correlation of the relative price of investment is remarkably robust to changes in parameter values. We also contribute to the international business-cycle literature by showing that financial frictions have the ability to increase the variance of the terms of trade as well as the international correlations of output, consumption, labour and investment.

Finally, we also considered risk shocks à la Christiano, Motto and Rostago (2014), who highlight the relative importance of risk shocks in generating realistic business-cycle volatility in a closed-economy framework. Our research suggests that in an international framework, risk shocks tend to move cross-country correlations away from what we observe in the data. Given the relative importance of risk shocks in a closed-economy model, their inability to drive international business cycles is striking. Further research is required to explore whether risk shocks can move economic aggregates together across countries.

8 Appendix

8.1 Data

The RPI is measured as the price deflator for investment goods divided by the price deflator for consumption goods. The variables considered in our consumption deflator include the consumption of non-durables, as well consumer services as listed in the National Income and Product Accounts (NIPA) provided by the U.S. Bureau of Economic Analysis. The investment deflator considered in this paper is the quality-adjusted price deflator for producer durable equipment calculated by Gordon (1990). Unlike equipment price deflators from the NIPA tables, Gordon's (1990) series is adjusted for changes in equipment quality, such as faster computer processing speeds or more energy-efficient vehicles, both of which expand the production possibility of equipment and, hence, the real value of these investment goods. Gordon's (1990) quality-adjusted investment price deflator is reported annually from 1949:1 until 1983. It is extended to span from 1949:1-2006:4 using Fisher's (2006) technique, which applies the work of Gordon's time series as well as that of Cummins and Violante (GCV) (2002) to expand the range of the dataset. Annual data are disaggregated into quarterly data via a splice interpolation.

The seasonally adjusted relative price of investment in the euro area from 1970:1 through to 2007:4 is obtained from the Area Wide Model dataset available through the Euro Area Business Cycle Network. It is calculated by dividing the price deflator for investment goods by the price deflator for consumption goods. Unlike the U.S. counterpart, this time series is not adjusted to allow for variation in the quality of capital goods. Furthermore, this time series calculates the RPI for all investment goods, rather than just equipment. Owing to these shortcomings, a similar time series is calculated for the United States using NIPA table data on the investment price deflator rather than the equipment price deflator as done above. This series, covering the same timespan as the euro-area RPI, is utilized for the calibration of the cross-country correlations in IST innovations (Section 5.1 in this paper). These data are made available via Ireland's (2013) academic website.

Data on the Baa-rated corporate bond rates as well as the 10-year rate on government bonds are obtained from the Federal Reserve Bank of St Louis' FRED database.

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Table 1

Parameter Values

Benchmark Calibration	
β	0.985
γ	2
ν	1.64
ψ	2.54658
η	0.1
ρ_z	0.95
ρ_s	0
$corr(\varepsilon_1, \varepsilon_2)$	0
σ_ε	$\sqrt{0.000139}$
δ	0.025
α_K	1/3
α_H	$1 - \alpha_K$
σ	0.5
$b_1/y_1 = a_2/y_2$	0.15
κ	0.9698
$\phi(\omega)$	lognormal$(1, \sigma_w^2)$
σ_w	0.207
Γ	0.947
μ	0.25

Table 2

Business-Cycle Statistics

	Data	Benchmark	No Fin. Frictions	IST Shocks	Risk Shocks
SD(GDP)	1.92	1.92	2.02	1.92	1.92
Correl(GDP_t, GDP_{t-1})	0.86	0.76	0.71	0.71	0.76
RelSD(C)	0.75	0.57	0.56	0.55	0.57
RelSD(H)	0.61	0.53	0.57	0.58	0.53
RelSD(I)	3.27	3.54	3.57	3.80	3.54
RelSD(TOT)	1.12^R, 1.92	1.74	1.47	1.58	1.75
RelSD(NX)	0.27, 0.30^R	0.27	0.27	0.28	0.27
RelSD(RPI)	0.15^{LW}, 0.39^{LW}	0.30	-	0.39	0.31
Correl(GDP, C)	0.82	0.97	0.98	0.96	0.97
Correl(GDP, H)	0.88	0.98	0.98	0.98	0.98
Correl(GDP, I)	0.94	0.96	0.97	0.94	0.96
Correl(GDP, NX)	-0.51^R, -0.37	-0.50	-0.54	-0.55	-0.50
Correl($GDP, NXQTY$)	-0.41^R	-0.15	-0.39	-0.36	-0.16
Correl(GDP, TOT)	-0.20, 0.12^R	0.45	0.50	0.38	0.45
Correl(GDP_1, GDP_2)	0.66	0.50	0.43	0.37	0.50
Correl(C_1, C_2)	0.51	0.21	0.17	0.17	0.21
Correl(I_1, I_2)	0.53	0.06	-0.04	-0.13	0.06
Correl(H_1, H_2)	0.33	0.46	0.37	0.29	0.45
Correl(RPI_1, RPI_2)	0.12^{LW}	0.25	-	0.12	0.25

Notes: SD(x)=standard deviation of x. RelSD(x)=SD(x)/SD(GDP). Correl(x, y)=correlation between x and y. Numbers in the "Data" columns are from BKK (1993), except for numbers with a superscript. Moments for the RPI (bearing superscript LW) are based on our own calculations using data described in Appendix. Numbers with superscript R are from Raffo (2008). For both NX and NXQTY, moments are calculated in levels.

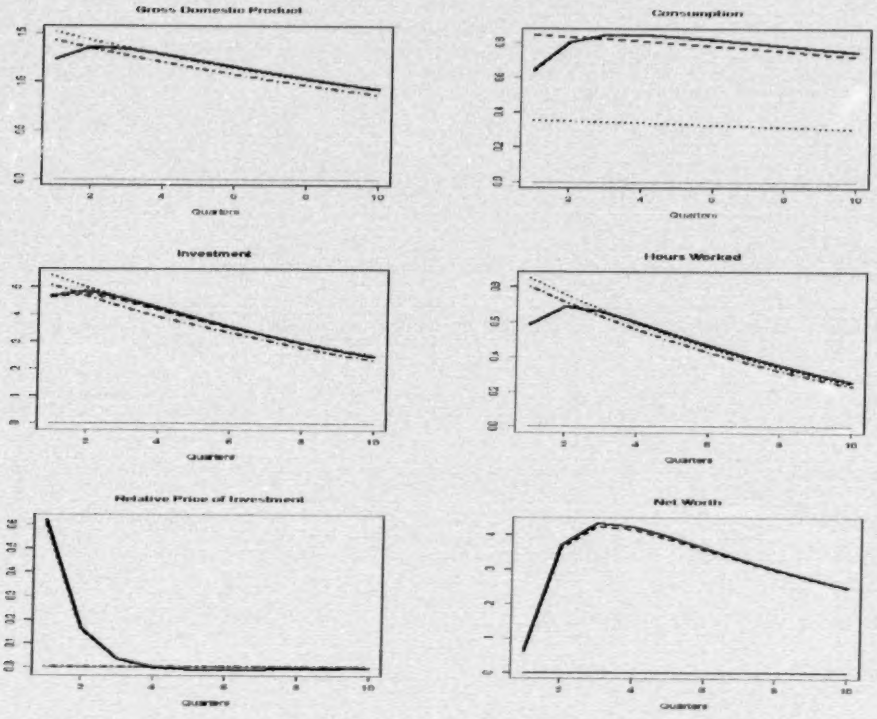
Table 3

Sensitivity Analysis

	Large Risk Shocks	$\eta = 1$	$\nu = 3$	$\sigma = 0.9$	$\rho_z = 0.97$ $\rho_s = 0.025$ $cor(\varepsilon_1, \varepsilon_2) = 0.29$
SD(GDP)	2.02	1.45	1.57	2.04	2.05
Cor(GDP_t, GDP_{t-1})	0.71	0.76	0.75	0.76	0.75
RelSD(C)	0.59	0.55	0.55	0.51	0.68
RelSD(H)	0.57	0.19	0.30	0.53	0.54
RelSD(I)	3.59	3.63	3.64	3.42	2.89
RelSD(TOT)	1.93	2.01	2.00	1.14	1.34
RelSD(NX)	0.27	0.27	0.28	0.14	0.21
RelSD(RPI)	0.72	0.29	0.31	0.28	0.24
Correl(GDP, C)	0.96	0.97	0.97	0.97	0.99
Correl(GDP, H)	0.97	0.94	0.99	0.99	0.98
Correl(GDP, I)	0.96	0.97	0.97	0.98	0.93
Correl(GDP, NX)	−0.54	−0.50	−0.51	−0.53	−0.40
Correl($GDP, NXQTY$)	−0.33	0.04	0.01	0.08	0.16
Correl(GDP, TOT)	0.21	0.47	0.48	0.51	0.36
Correl(GDP_1, GDP_2)	0.37	0.50	0.48	0.33	0.68
Correl(C_1, C_2)	0.07	0.17	0.14	0.32	0.67
Correl(I_1, I_2)	−0.05	0.08	0.06	0.01	0.07
Correl(H_1, H_2)	0.22	0.72	0.47	0.33	0.66
Cor(RPI_1, RPI_2)	0.25	0.24	0.21	0.29	0.26

Figure 1

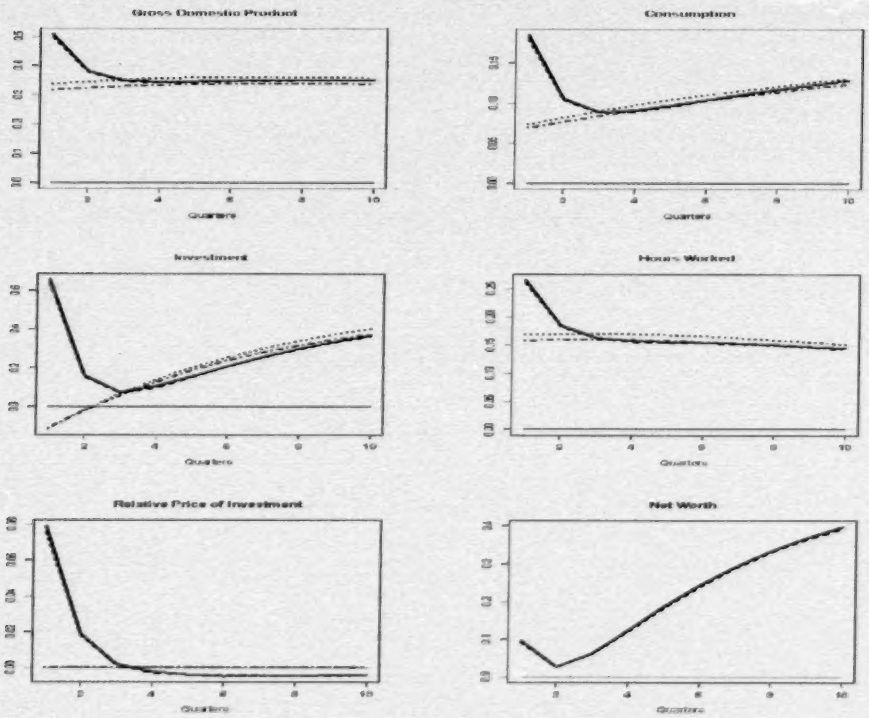
Impulse Responses to Home Country TFP Shock:
Home Country



Impulse responses to a one-standard-error innovation to ϵ_t^Z for the benchmark model (solid), the model with risk shocks (dashed), a model with financial frictions removed (dotted), and the IST model (dot dash). Each variable is measured as a percentage deviation from its steady state.

Figure 2

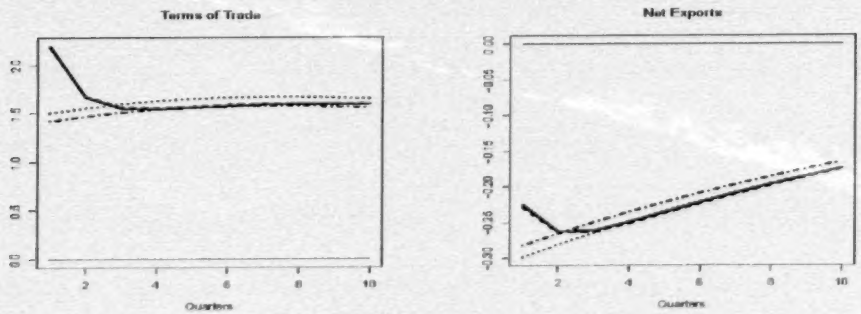
Impulse Responses to Home Country TFP Shock:
Foreign Country



Impulse responses to a one-standard-error innovation to ϵ_t^Z for the benchmark model (solid), the model with risk shocks (dashed), a model with financial frictions removed (dotted), and the IST model (dot dash). Each variable is measured as a percentage deviation from its steady state.

Figure 3

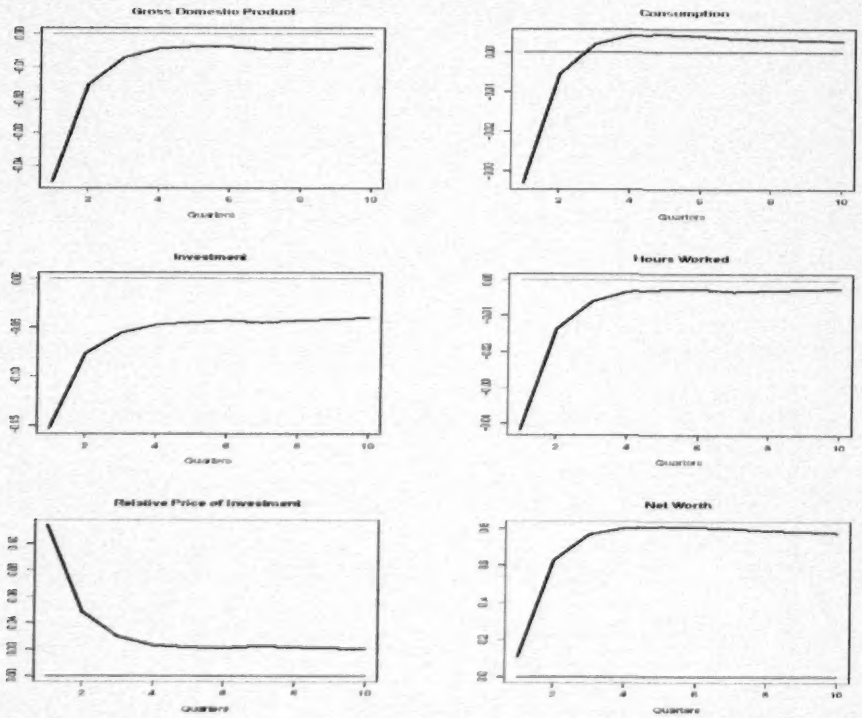
Impulse Responses to Home Country TFP Shock
Home Country's Terms of Trade and Net Exports



Impulse responses to a one-standard-error innovation to ϵ_t^Z for the benchmark model (solid), the model with risk shocks (dashed), a model with financial frictions removed (dotted), and the IST model (dot dash). Each variable is measured as a percentage deviation from its steady state.

Figure 4

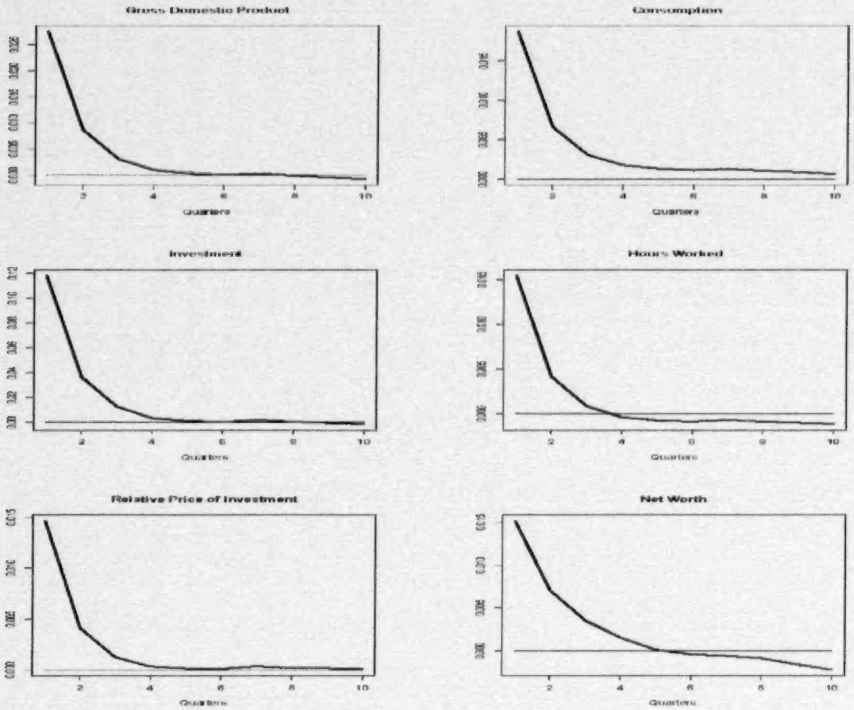
Impulse Responses to Home Country Risk Shock:
Home Country



Impulse responses to a one-standard-error innovation to ϵ_t^{Risk} for the benchmark model. Each variable is measured as a percentage deviation from its steady state.

Figure 5

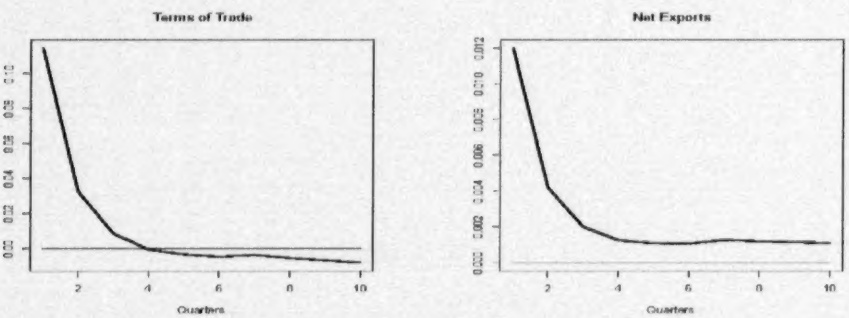
Impulse Responses to Home Country Risk Shock:
Foreign Country



Impulse responses to a one-standard-error innovation to ϵ_t^{Risk} for the risk-shock model. Each variable is measured as a percentage deviation from its steady state.

Figure 6

Impulse Responses to Home Country Risk Shock:
Home Country's Terms of Trade and Net Exports

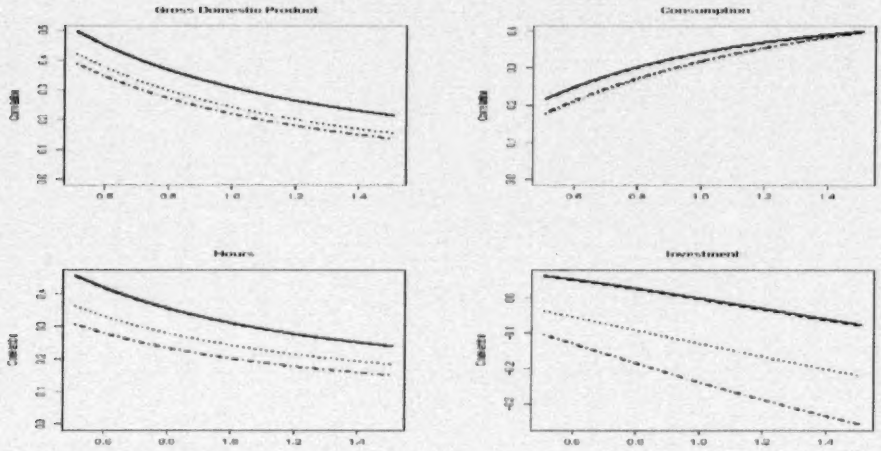


Impulse responses to a one-standard-error innovation to ϵ_t^{Risk} for the risk-shock model. Each variable is measured as a percentage deviation from its steady state.

Figure 7

Cross-Country Correlation

Sensitivity to the Elasticity of Substitution

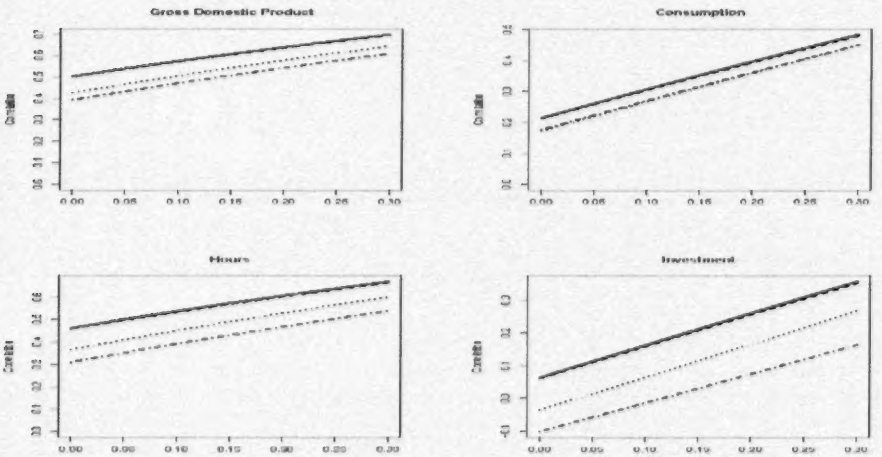


Cross-country correlations are calculated for the benchmark model (solid), a model with risk shocks (dashed), a model with financial frictions removed (dotted) and, last of all, the IST model (dot dash).

Figure 8

Cross-Country Correlation

Sensitivity to Correlated Technologies

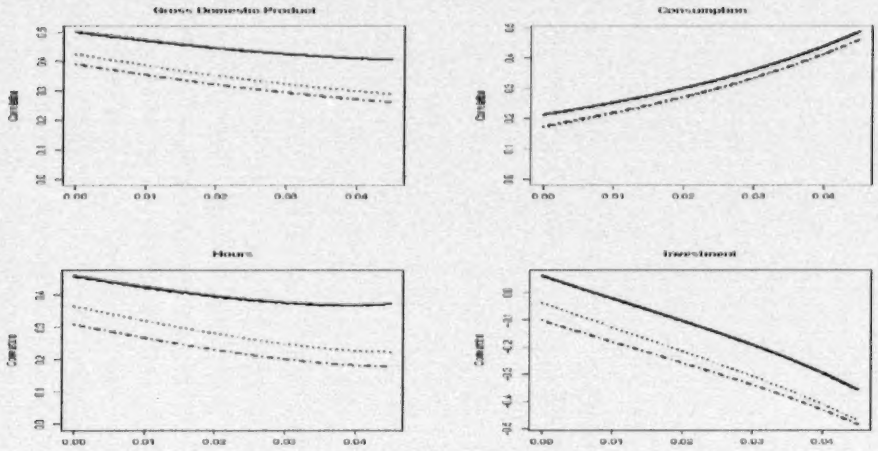


Cross-country correlations are calculated for the benchmark model (solid), a model with risk shocks (dashed), a model with financial frictions removed (dotted) and, last of all, the IST model (dot dash).

Figure 9

Cross-Country Correlation

Sensitivity to Technology Spillovers

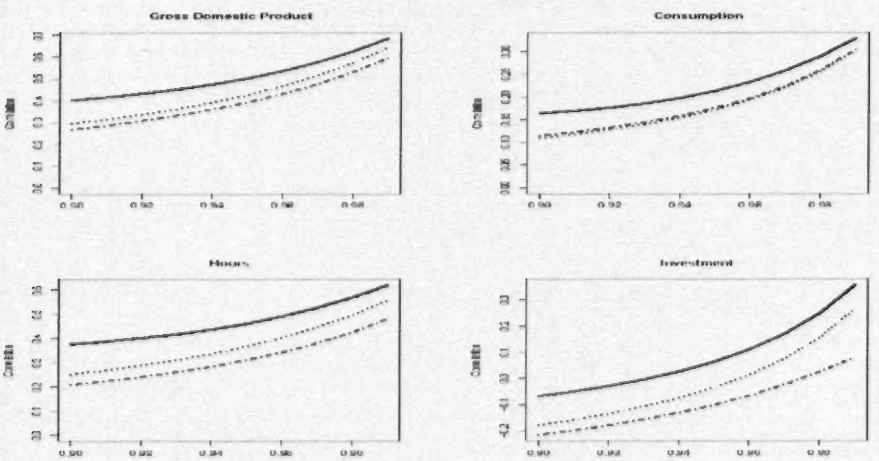


Cross-country correlations are calculated for the benchmark model (solid), a model with risk shocks (dashed), a model with financial frictions removed (dotted) and, last of all, the IST model (dot dash).

Figure 10

Cross-Country Correlation

Sensitivity to Technology Persistence



Cross-country correlations are calculated for the benchmark model (solid), a model with risk shocks (dashed), a model with financial frictions removed (dotted) and, last of all, the IST model (dot dash).